

Gov 50: 8. Measurement: Summarizing Bivariate Relationships

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Fall 2018

1. Today's agenda

2. Investigating fraud

3. Bivariate relationships

1/ Today's agenda

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- Midterm course evaluations after the midterm.

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 - ▶ panel data: baseline plus 6 waves.

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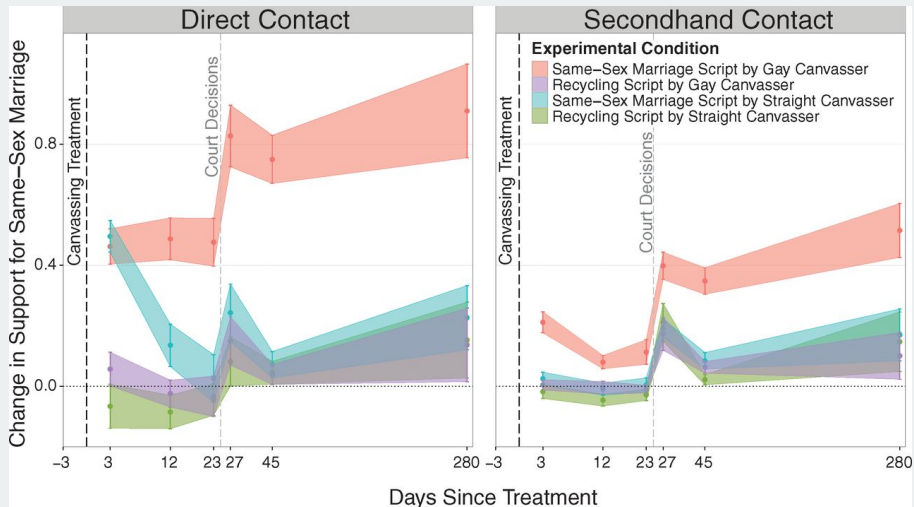
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- Outcome measures:
 - ▶ support for same-sex marriage.
 - ▶ feeling toward gay people.

Big and lasting effects of persuasion



Reshaped data

Name	Description
<code>study</code>	Which study is the data from (1 = Study1, 2 = Study2)
<code>treatment</code>	Five possible treatment assignment options
<code>therm1</code>	Survey thermometer rating of feeling towards gay couples in waves 1 (0–100)
<code>therm2</code>	Survey thermometer rating of feeling towards gay couples in waves 2 (0–100)
<code>therm3</code>	Survey thermometer rating of feeling towards gay couples in waves 3 (0–100)
<code>therm4</code>	Survey thermometer rating of feeling towards gay couples in waves 4 (0–100)

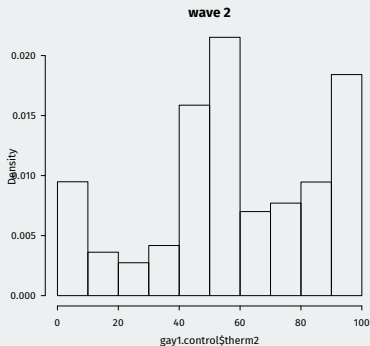
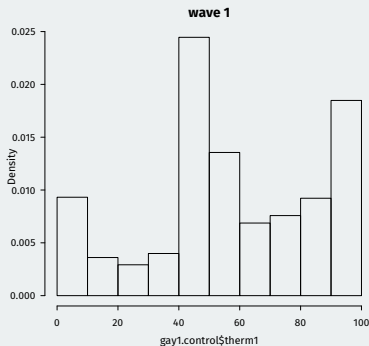
```
gay.reshaped <- read.csv("data/gayreshaped.csv")
names(gay.reshaped)
```

```
## [1] "study"      "treatment" "therm1"     "therm2"
## [5] "therm3"     "therm4"
```

Comparison of gay thermometer across waves

- Compare between waves 1 and 2 for the control group in Study 1:

```
gay1.control <- subset(gay.resshaped, (study == 1) &  
                        (treatment == "No Contact"))  
hist(gay1.control$therm1, freq = FALSE, main = "wave 1")  
hist(gay1.control$therm2, freq = FALSE, main = "wave 2")
```



3/ Bivariate relationships

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```
plot(x = gay1.control$therm1, y = gay1.control$therm2,  
     xlab = "Wave 1", ylab = "Wave 2")
```


Scatterplot

```
gay1.control[1, c("therm1", "therm2")]
```

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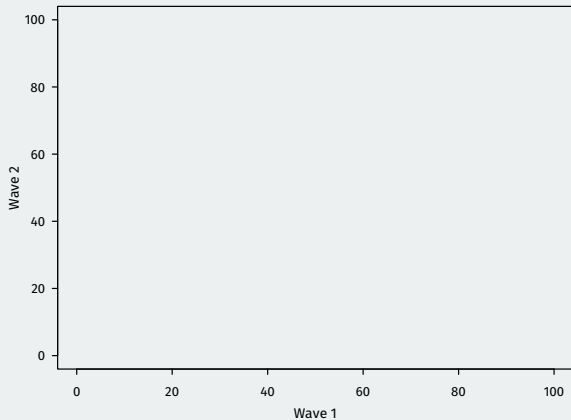
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##   therm1 therm2  
## 1     91     91
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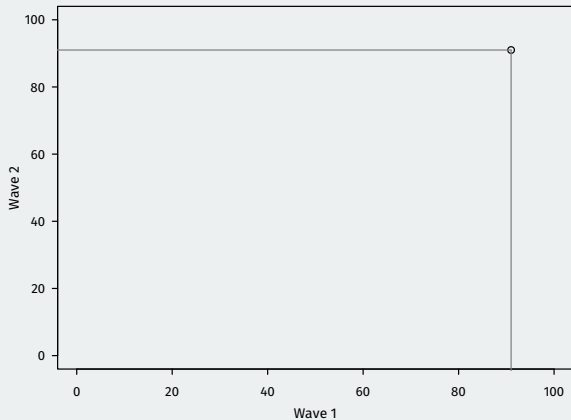
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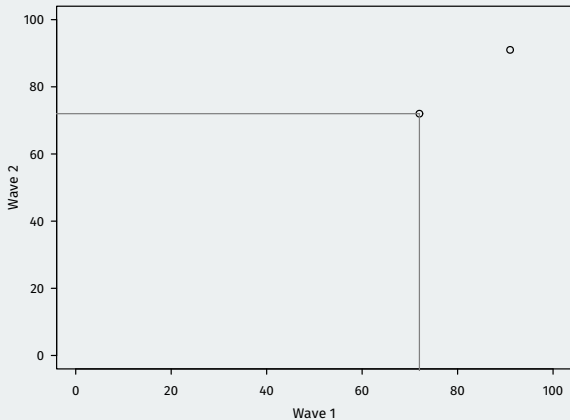
```
##   therm1 therm2  
## 1     91     91
```



Scatterplot

```
gay1.control[2, c("therm1", "therm2")]
```

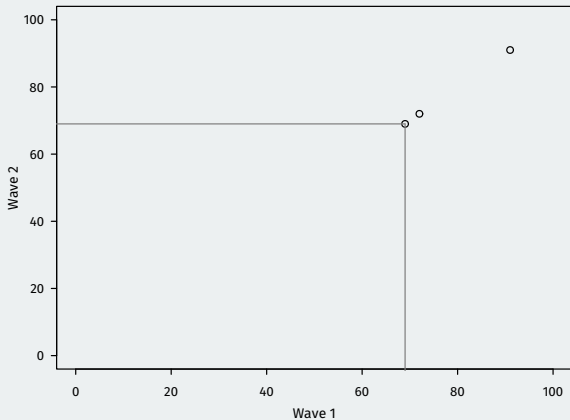
```
##   therm1 therm2  
## 2     72     72
```



Scatterplot

```
gay1.control[3, c("therm1", "therm2")]
```

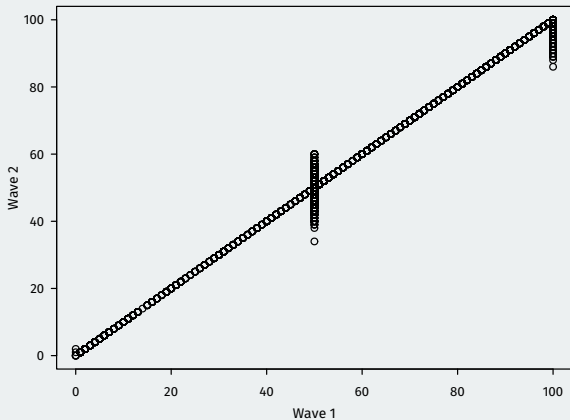
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##   therm1 therm2  
## 3      69      69
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- **z-score:**

$$\text{z-score of } x_i = \frac{x_i - \text{mean of } x}{\text{standard deviation of } x}$$

- z-scores don't depend on units:

$$\text{z-score of } (ax_i + b) = \text{z-score of } x_i$$

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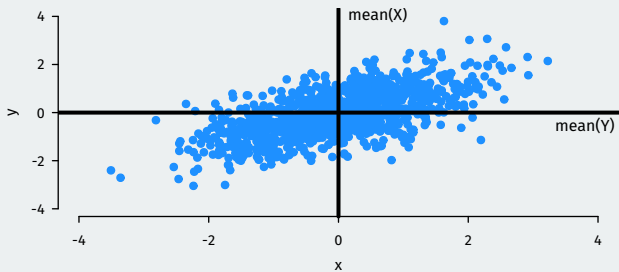
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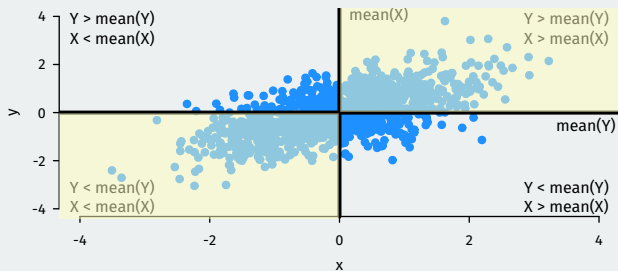
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- The technical definition of the **correlation coefficient**:

$$\frac{1}{n-1} \sum_{i=1}^n [(z\text{-score for } x_i) \times (z\text{-score for } y_i)]$$

Correlation intuition

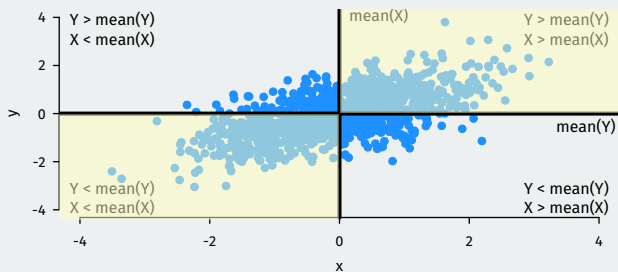


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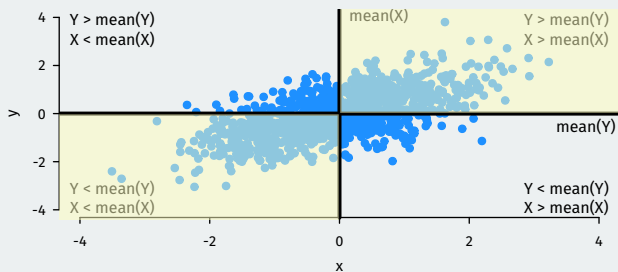
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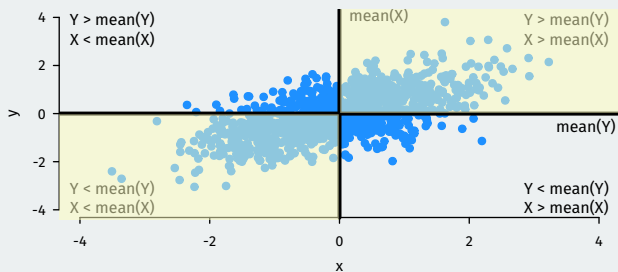
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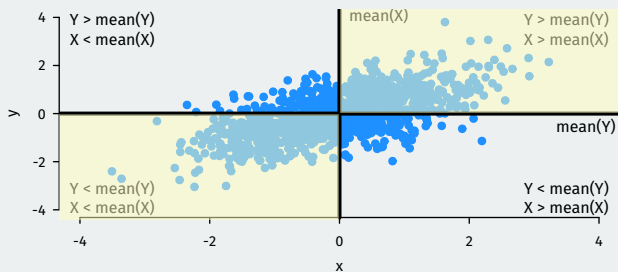
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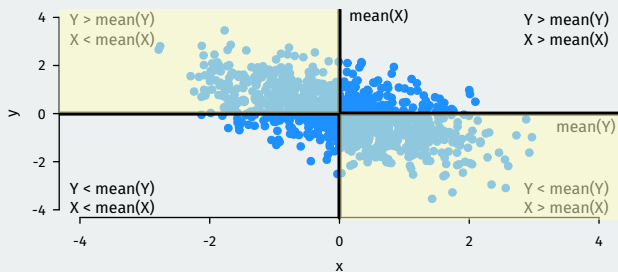
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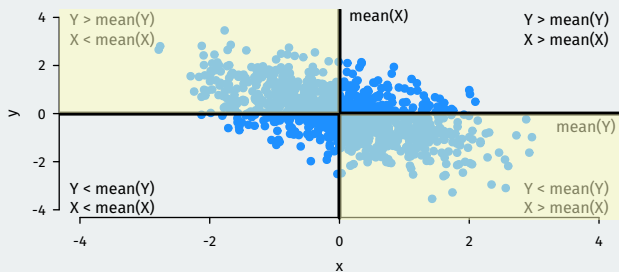
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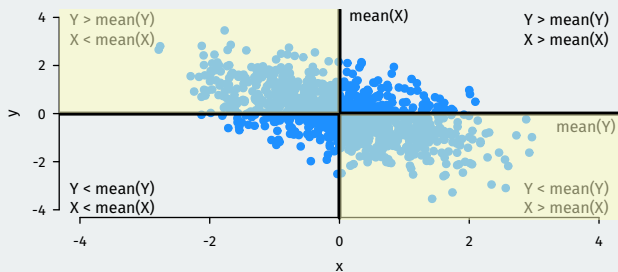
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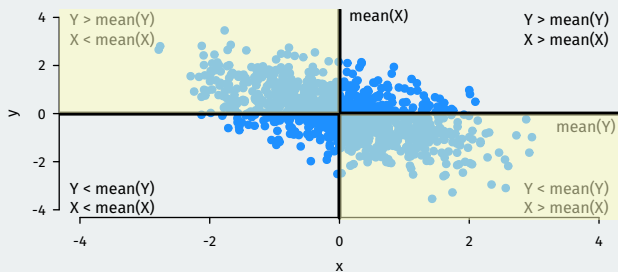
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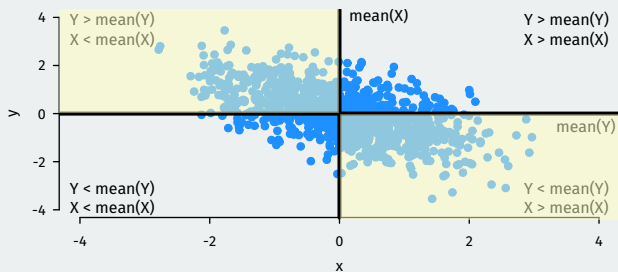
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 - ▶ Celsius vs. Fahrenheit; dollars vs. pesos; cm vs. in.

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```
cor(gay1.control$therm1, gay1.control$therm2,  
    use = "pairwise")
```

```
## [1] 0.998
```

Correlation in R

- Use the `cor()` function
- Missing values: set the `use = "pairwise"` \rightsquigarrow available case analysis

```
cor(gay1.control$therm1, gay1.control$therm2,  
     use = "pairwise")
```

```
## [1] 0.998
```

- Extremely high correlation!

Comparisons between studies

- Cannot use `plot()` or `cor()`. Why?

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```
gay1 <- subset(gay.resshaped, (study == 1))  
gay2 <- subset(gay.resshaped, (study == 2))
```

Comparisons between studies

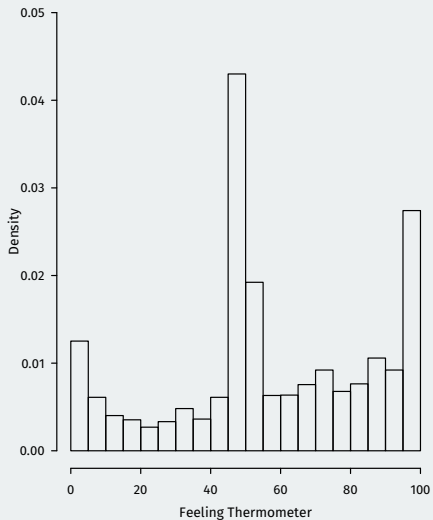
- Cannot use `plot()` or `cor()`. Why?
- Different studies have different respondents.
- Start with histograms:

```
gay1 <- subset(gay.reshaped, (study == 1))  
gay2 <- subset(gay.reshaped, (study == 2))
```

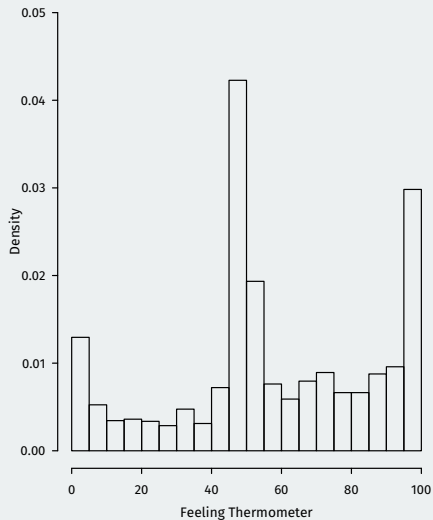
```
hist(gay1$therm1, freq = FALSE, breaks = 20,  
     ylim = c(0, 0.05), xlab = "Feeling Thermometer",  
     main = "Study 1, Baseline")  
hist(gay2$therm1, freq = FALSE, breaks = 20,  
     ylim = c(0, 0.05), xlab = "Feeling Thermometer",  
     main = "Study 2, Baseline")
```


Very similar!!

Study 1, Baseline



Study 2, Baseline



Quantile-Quantile Plot

- **Quantile-quantile plot (qq-plot):** Plot the **quantiles** of each distribution against each other.

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 - ▶ (min of X , min of Y)
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Quantile-Quantile Plot

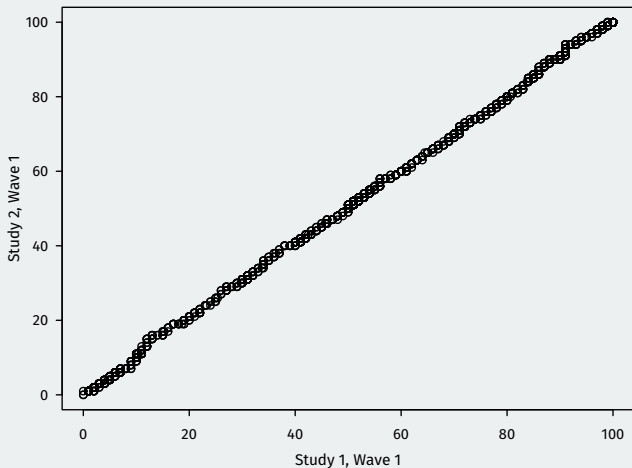
- **Quantile-quantile plot (qq-plot):** Plot the **quantiles** of each distribution against each other.
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Quantile-Quantile Plot

- **Quantile-quantile plot (qq-plot):** Plot the **quantiles** of each distribution against each other.
- Example points:
 - ▶ (min of X , min of Y)
 - ▶ (median of X , median of Y)
 - ▶ (25th percentile of X , 25th percentile of Y)
- 45 degree line indicates quality of the two distributions.

QQ-plot example

```
qqplot(gay1$therm1, gay2$therm1, xlab = "Study 1, Wave 1",  
       ylab = "Study 2, Wave 1")
```



What is going on?!?!?

- Question wording of thermometer score attributed to 2012 Cooperative Campaign Analysis Project (CCAP):

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```
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mean(is.na(ccap$gaytherm))
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```

```
## [1] 0.0704
```

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```
## [1] 0.0704
```

```
mean(is.na(gay1$therm1))
```

What is going on?!?

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ccap <- read.csv("data/ccap2012.csv")
mean(is.na(ccap$gaytherm))
```

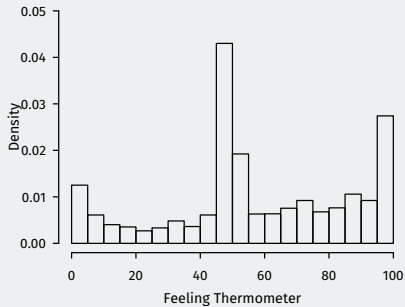
```
## [1] 0.0704
```

```
mean(is.na(gay1$therm1))
```

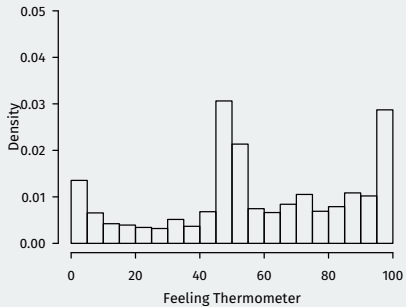
```
## [1] 0
```

Comparison of CCAP and Study 1

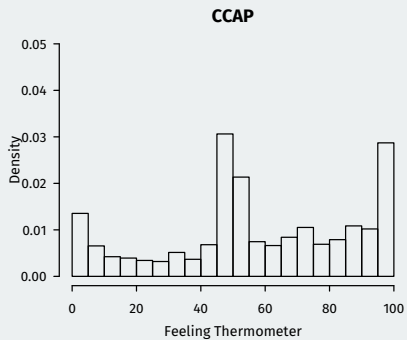
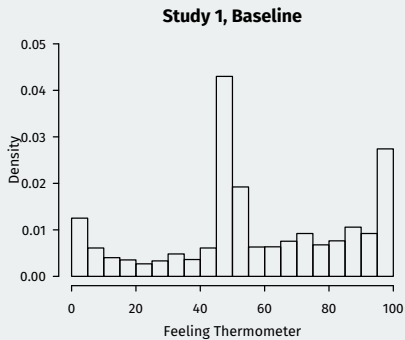
Study 1, Baseline



CCAP

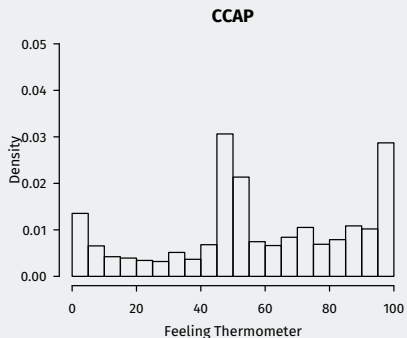
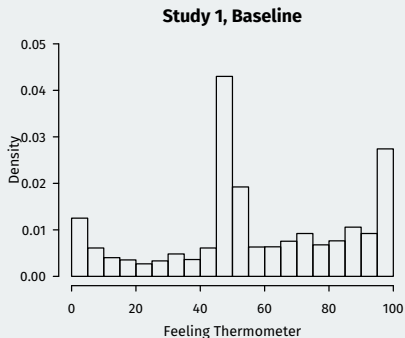


Comparison of CCAP and Study 1



- Suspiciously similar!

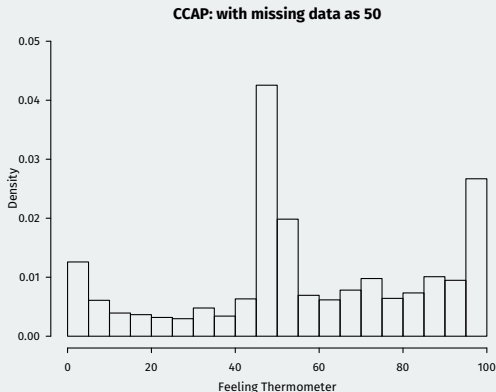
Comparison of CCAP and Study 1



- Suspiciously similar!
- What's the difference?

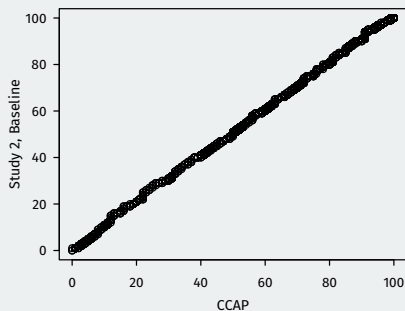
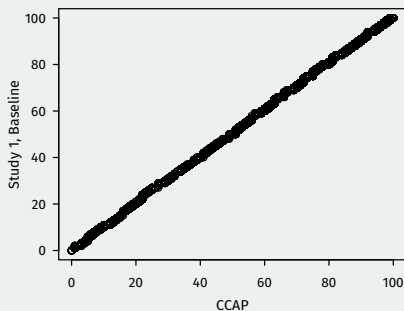
Recoding missing as 50s

```
ccap$gaytherm[is.na(ccap$gaytherm)] <- 50
hist(ccap$gaytherm, freq = FALSE,
     ylim = c(0, 0.05), xlab = "Feeling Thermometer",
     main = "CCAP: with missing data as 50")
```



QQ plots reveal extreme similarity

```
qqplot(ccap$gaytherm, gay1$therm1, xlab = "CCAP",  
       ylab = "Study 1, Baseline")  
qqplot(ccap$gaytherm, gay2$therm1, xlab = "CCAP",  
       ylab = "Study 2, Baseline")
```



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By BENEDICT CAREY and PAM BELLUCK MAY 25, 2015



Donald P. Green, left, a co-author of a challenged study by Michael LaCour, right, from Mr. LaCour's Facebook page.



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Wrapping up

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- After midterm: prediction!